

Units

$$\text{arcsec} := \frac{\text{deg}}{60 \cdot 60}$$

Definition of an arcsecond

$$":=\text{arcsec}$$

Common abbreviation for an arcsecond

$$M_{\oplus} := 5.9736 \cdot 10^{24} \cdot \text{kg}$$

Mass of the Earth

$$\text{AU} := 1.49597870700 \cdot 10^8 \cdot \text{km}$$

Definition of Earth-Sun Distance

$$L_{\odot} := 3.846 \cdot 10^{26} \text{W}$$

Luminosity of the Sun

$$R_{\text{J}} := 43441 \text{m}$$

Radius of Jupiter

$$M_{\text{J}} := 317.8 \cdot M_{\oplus}$$

Mass of Jupiter

$$\text{ly} := c \cdot \text{yr} = 9460528404879 \cdot \text{km}$$

Definition of light-year

$$\text{pc} := \frac{\text{AU}}{\text{arcsec}} = 3 \cdot \text{ly}$$

Definition of parsec. Common unit of distance for astronomers.

$$M_{\odot} := 1.989 \cdot 10^{30} \text{kg}$$

Mass of the Sun

Constants

$$G_U := 6.6742 \cdot 10^{-11} \cdot \frac{\text{m}^3}{\text{kg} \cdot \text{sec}^2}$$

Universal gravitational constant

$$\sigma := 5.670400 \cdot 10^{-8} \cdot \frac{\text{watt}}{\text{m}^2 \cdot \text{K}^4}$$

Stefan-Boltzmann Constant

[Link](#)

Utility Functions

Period of an Exoplanet **Uses Kepler's Third Law**

$$m_P \cdot \omega^2 \cdot d = G_U \cdot \frac{m_P \cdot M_S}{d^2}$$

substitute, $\omega = \frac{2 \cdot \pi}{T_P}$
 assume, ALL > 0 $\rightarrow \frac{2 \cdot \pi \cdot d^{\frac{3}{2}}}{\sqrt{G_U} \cdot \sqrt{M_S}}$
 solve, T_P

$$T_P(M_S, d) := \frac{2 \cdot \pi \cdot d^{\frac{3}{2}}}{\sqrt{G_U} \cdot \sqrt{M_S}}$$

Radius of a Exoplanet **Uses the Effective Temperature of the Exoplanet**

$$L_{\text{Star}} = 4 \cdot \pi \cdot R_P^2 \cdot \sigma \cdot T_{\text{eff}}^4$$

assume, ALL > 0
 solve, R_P $\rightarrow \frac{\sqrt{L_{\text{Star}}}}{2 \cdot \sqrt{\pi} \cdot T_{\text{eff}}^2 \cdot \sqrt{\sigma}}$

$$R_P(L_{\text{Star}}, T_{\text{eff}}) := \frac{\sqrt{L_{\text{Star}}}}{2 \cdot \sqrt{\pi} \cdot T_{\text{eff}}^2 \cdot \sqrt{\sigma}}$$

Mass of an Exoplanet **Uses the Surface Gravity of the Exoplanet**

$$g_P = \frac{G_U \cdot M_P}{R_P^2}$$

assume, ALL > 0
 solve, M_P $\rightarrow \frac{R_P^2 \cdot g_P}{G_U}$

$$M_P(R_P, g_P) := \frac{R_P^2 \cdot g_P}{G_U}$$

Analysis

Measurements

$M_{CVSO30} := 0.39 \cdot M_{\odot}$ Mass of CV30 relative to our Sun.

$d_{CVSO} := 330 \text{ pc}$ Distance to CV30 from the Sun.

$L_{CVSO30c} := 10^{-3.78} \cdot L_{\odot}$ Luminosity of CV30c relative to the Sun.

$\theta_{CVSO30c} := 1.85 \cdot "$ Maximum angular separation between the CV30c and CV30.

$T_{CVSOc} := 1600 \text{ K}$

$g_{CVSO30c} := 10^{3.6} \cdot \frac{\text{cm}}{\text{s}^2}$ Estimate of CV30c's surface gravity from spectral measurements.

Computation of Planet Characteristics

$T_{CVSOc} := T_P(M_{CVSO30}, d_{CVSOc}) = 27100 \text{ yr}$ ✓
CVSOc Orbital Period. The published value is 27,100 years.

$d_{CVSOc} := \theta_{CVSO30c} \cdot d_{CVSO} = 660 \text{ AU}$ ✓
Compute distance of CVSO30c from CVSO30. The published value is 660 AU.

$R_{CVSO30c} := R_P(L_{CVSO30c}, T_{CVSOc}) = 1.67 \cdot R_{Jup}$ ✓
Radius of CVSOc. Published value is 1.63 times Jupiter's radius..

$M_{CVSOc} := M_P(R_{CVSO30c}, g_{CVSO30c}) = 4.3 \cdot M_{Jup}$ ✓
Mass of CVSOc. Published value is 4.3 times Jupiter's mass.